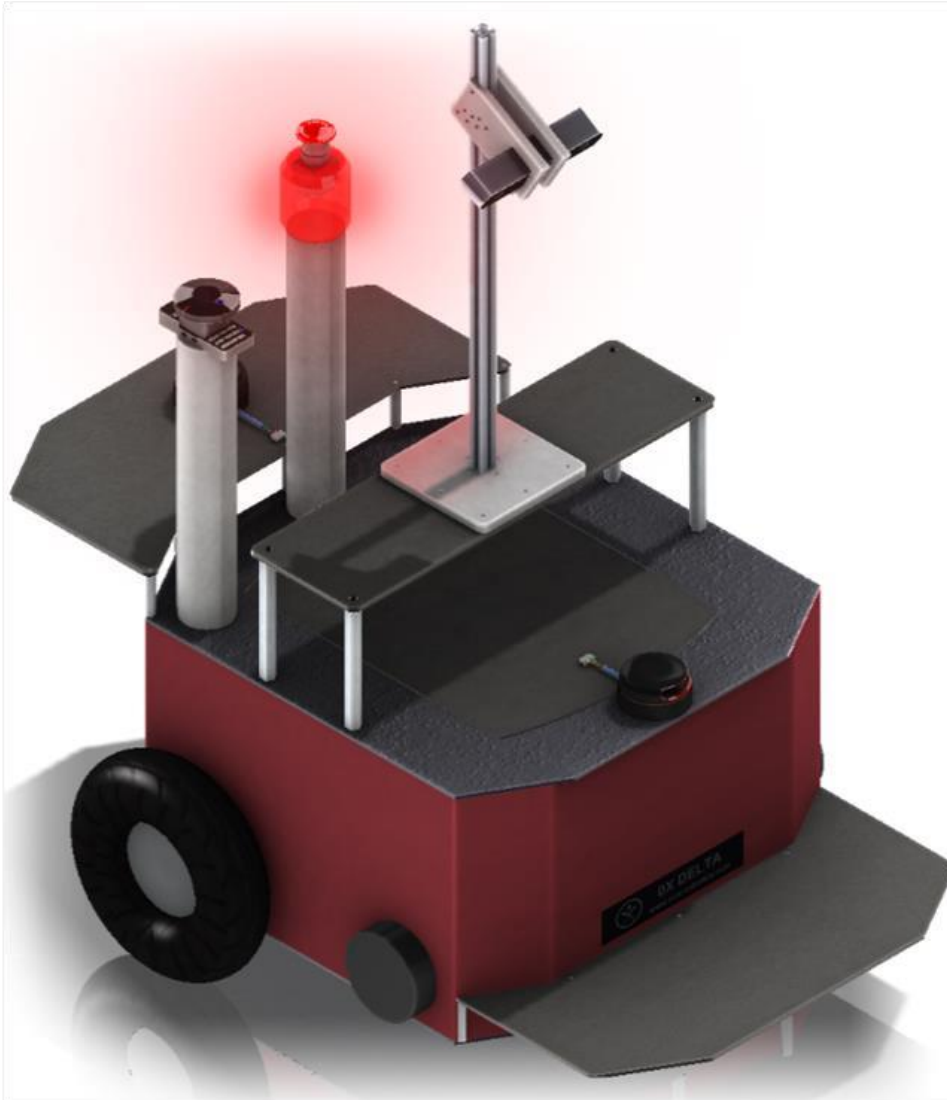


# Autonomous Navigation



Mangal Kothari  
Department of Aerospace Engineering  
Indian Institute of Technology Kanpur

Kanpur – 208016

[mangal@iitk.ac.in](mailto:mangal@iitk.ac.in)

9460255282

Class Timing: M-12:00-13:15

T-09:00-10:15

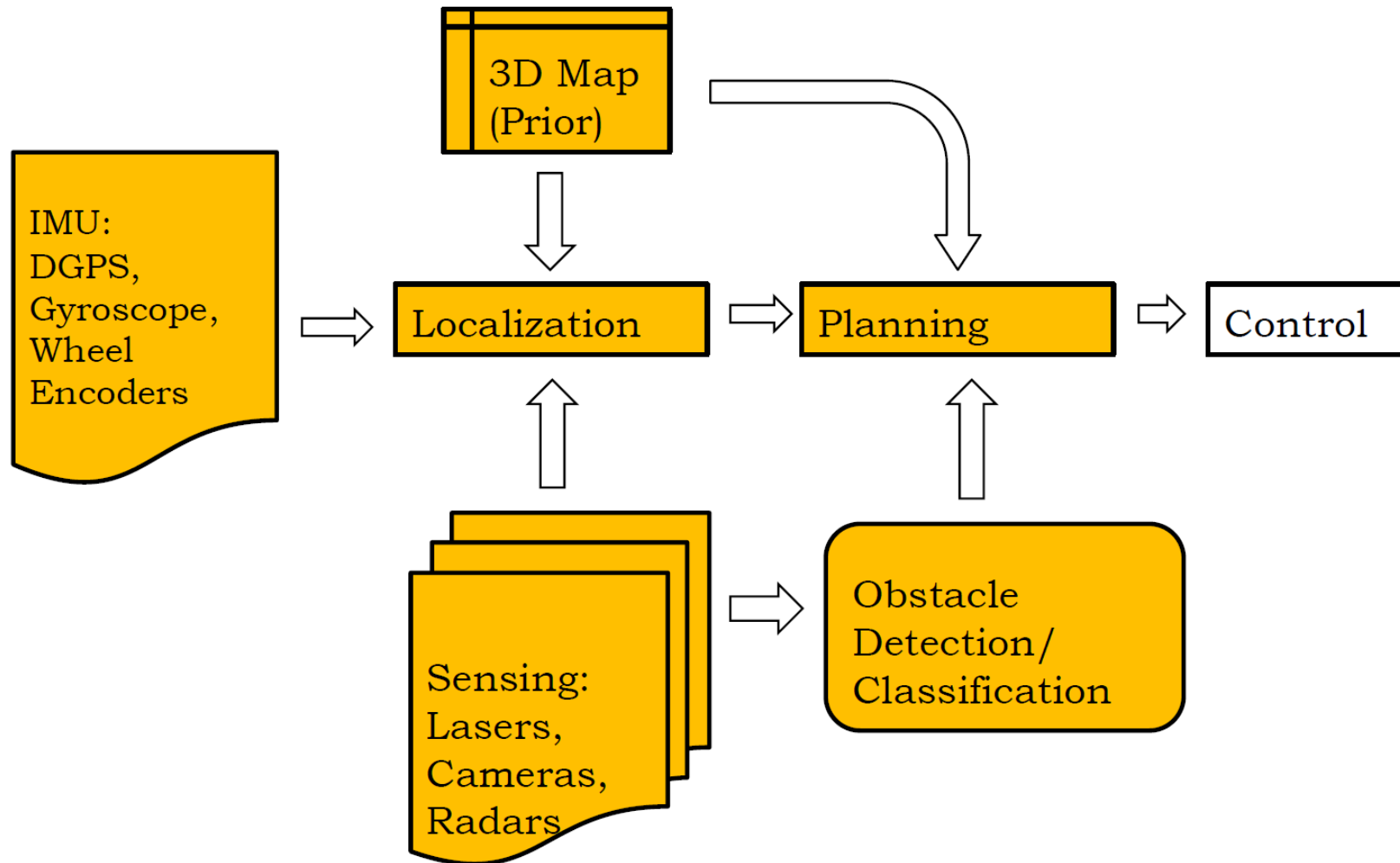
TA: Mr. Aalap A Saha

# Autonomous Navigation



I I T K A N P U R

## Autonomous Navigation System



# Course Content



- Introduction: practical examples and challenges – IGVC, SAVe, Mehar Baba competition
- ROS and state estimation (Bayesian filter-Kalman Filter, Extended Kalman Filter, Unscented Kalman Filter), Nonparametric filter (particle filter), Localization, SLAM, Cooperative localization
- Path planning algorithms: Deterministic and probabilistic algorithms, Task allocation algorithms
- Vision and communication systems
- Topics can be added and removed based on **feedback!!!**

# Reference



- Probabilistic Robotics. Sebastian Thrun, Wolfram Burgard and Dieter Fox. MIT press, 2005.
- Principles of Robot Motion: Theory, Algorithms and Implementations, Howie Choset *et al.*. MIT Press, 2005.
- State Estimation for Robotics: Timothy D. Barfoot. Cambridge University Press, 2017.
- A Gentle Introduction to ROS: Jason M. O’Kane. 2013.

# Evaluation

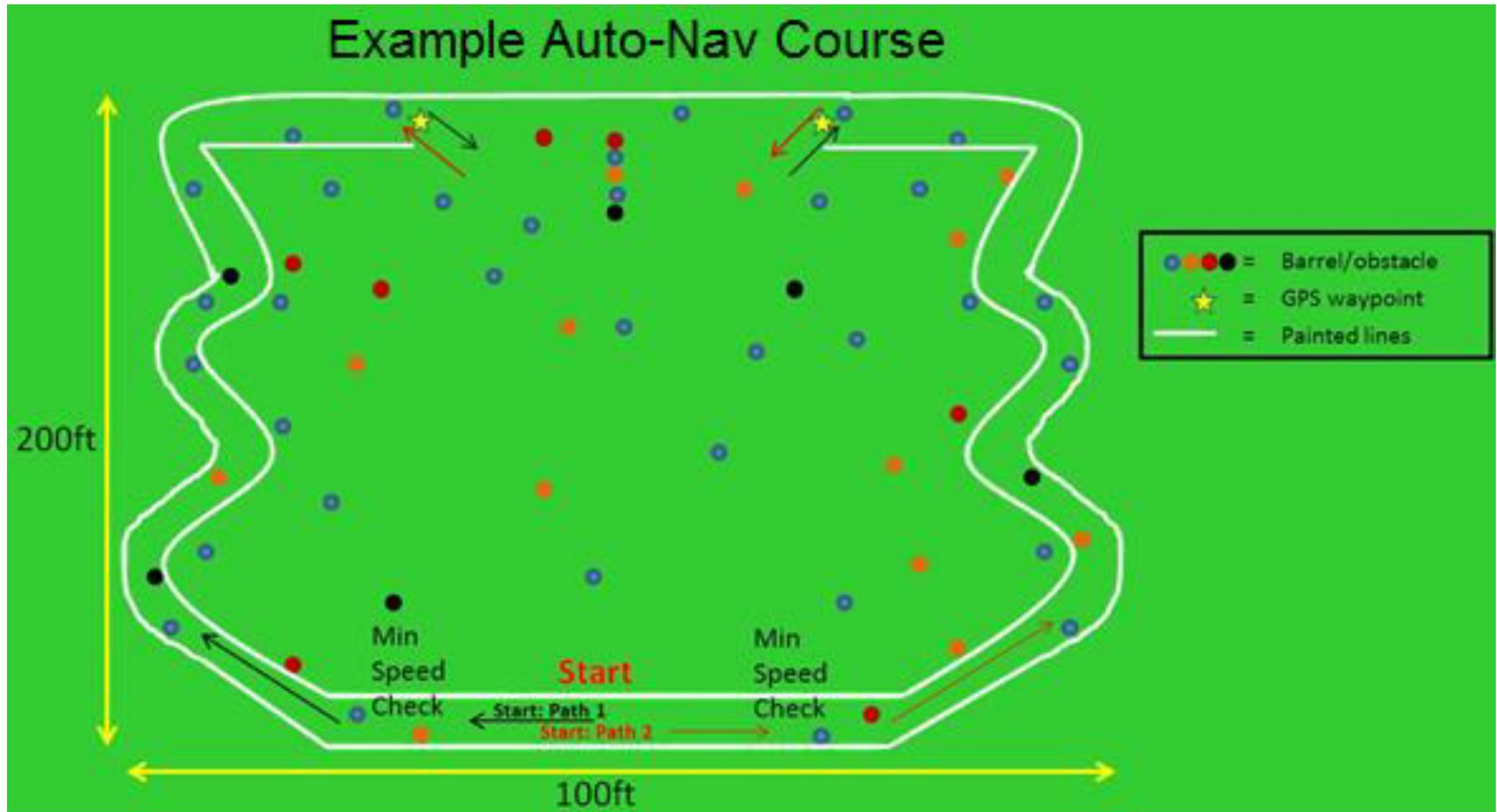


- 
- **Assignment – 40%**
  - **Project (maximum 3 students) – 40%**
  - **Midterm exam – 10%**
  - **Quizzes (after midsem) – 10%**
  - **Plagiarism – de-register/failed**

# Problem Statement



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# Specifications



- **Length: Min 3 feet, Max 7 feet**
- **Width: Min 2 feet, Max 4 feet**
- **Height: Max 6 feet**
- **Propulsion: Battery powered**
- **Average speed: 1 mph**
- **Minimum speed: 1 mph for the first 44 feet**
- **Maximum speed: 5 mph**
- **Mechanical E stop: Hardware base**
- **Wireless stop: Effective with in 100 feet**
- **Safety light: Must be on when vehicle is on**
- **Payload: 20 pounds, 18"x8"x8"**

# Qualification



- 
- **Mechanical stop and E stop evaluation**
  - **Lane following (with U turn)**
  - **Obstacle avoidance**
  - **Waypoint following**



# Intelligent Ground Vehicle Competition (IGVC)



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## IGVC 2018 GPS Waypoints

North	42.6791159989	-83.1949250546
Midpoint	42.6789603912	-83.1951132036
South	42.6788151958	-83.1949093082
Practice1	42.6783260449	-83.1946867275
Practice2	42.6781974127	-83.1949338822
Qualification2	42.6778987274	-83.1954820799

# Vehicle Model

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- Compact design
- Switchable vehicle design
- Spring based suspension system
- Height and angle adjustable camera mount

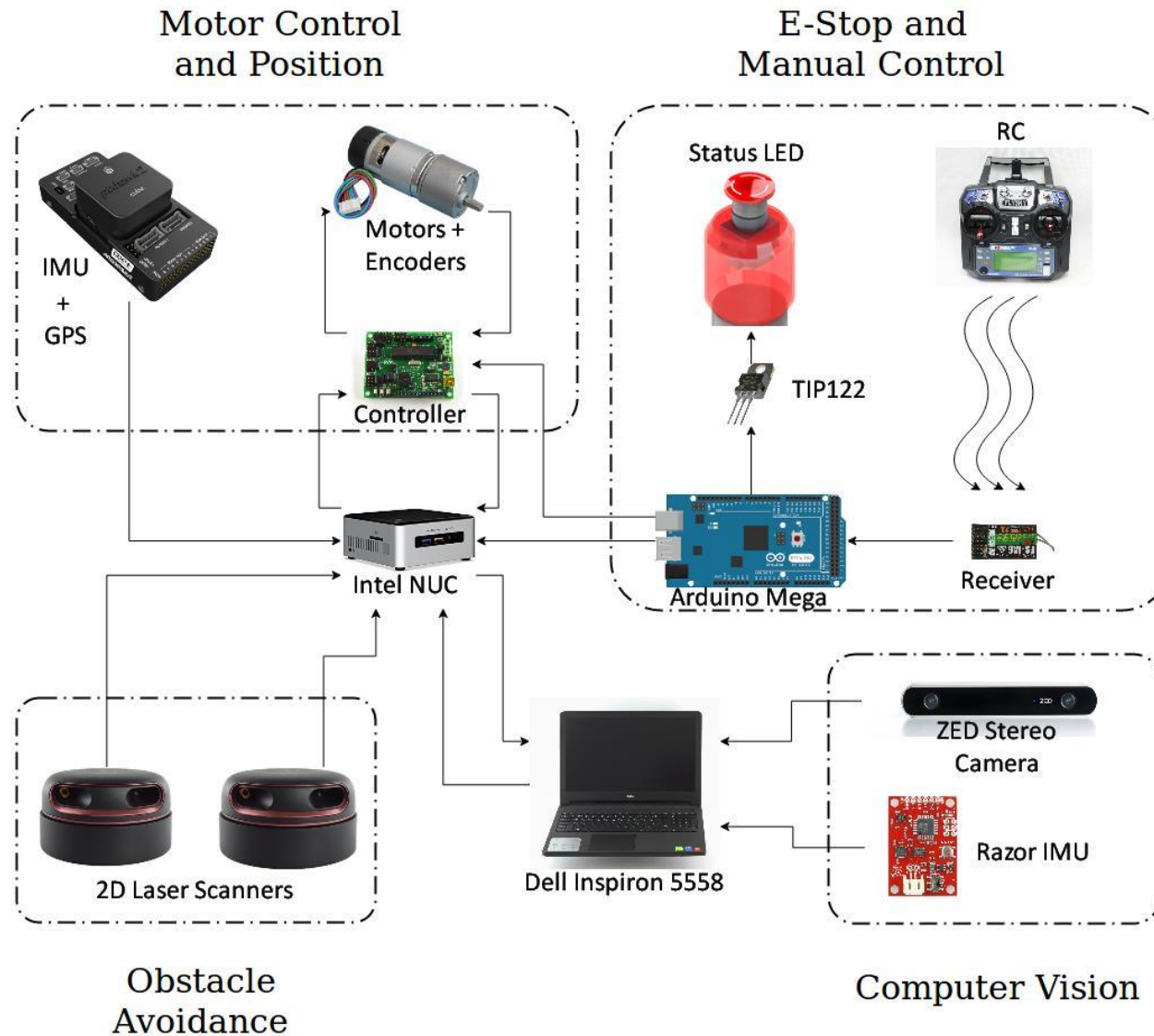




# System Architecture



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# Robot Operating Systems



- 
- **A meta operating system for robot**
  - **A collection of packaging, software building tools**
  - **An architecture for distributed interprocess/ inter-machine communication and configuration**
  - **A language-independent architecture (C++, python, lisp, java, and more)**

# ROS Communication Layer: ROS Core

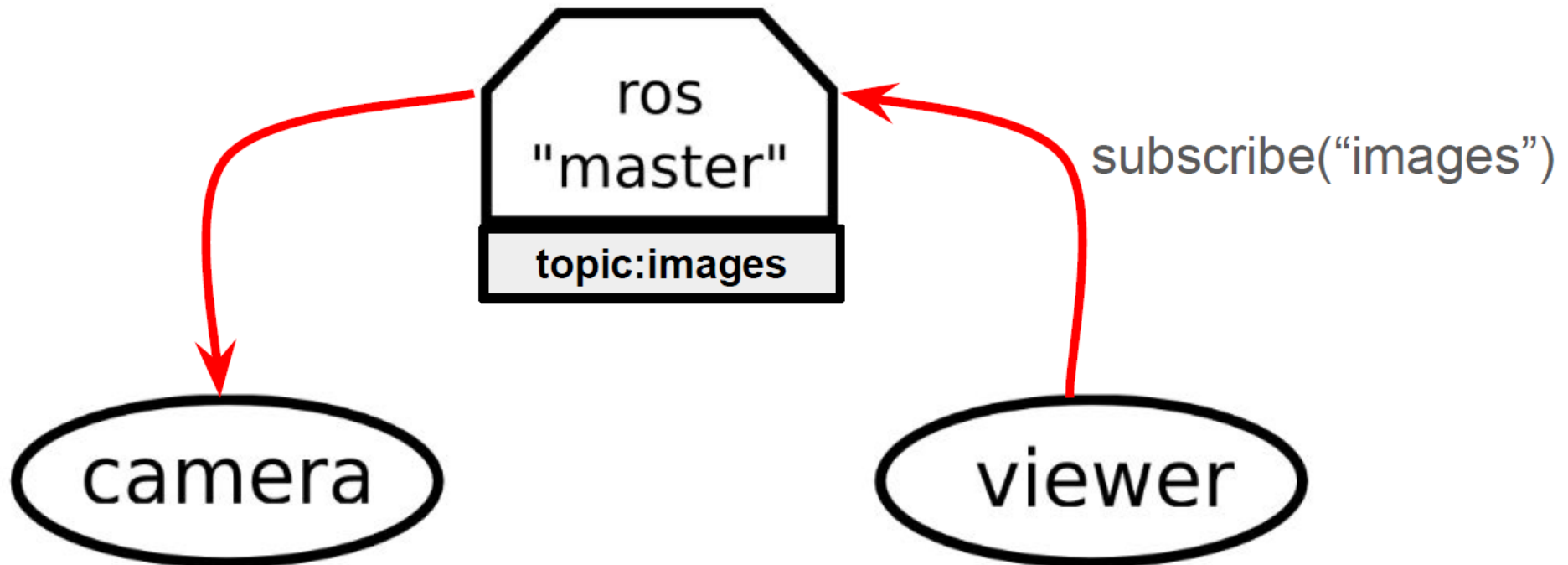


- **ROS master**
  - Centralized communication server based on XML and RPC
  - Registers and looks up names for ROS graph resources
- **Nodes**
  - Distributed process over the network (executable runs a separate thread)
  - Serve as source and sink for data
- **Topics**
  - Asynchronous many-to-many communication
  - Publish and subscribe structure

# Asynchronous Distributed Communication



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## ROS Master

Manage communication among nodes

Every node register when at start up with the master

\$ roscore

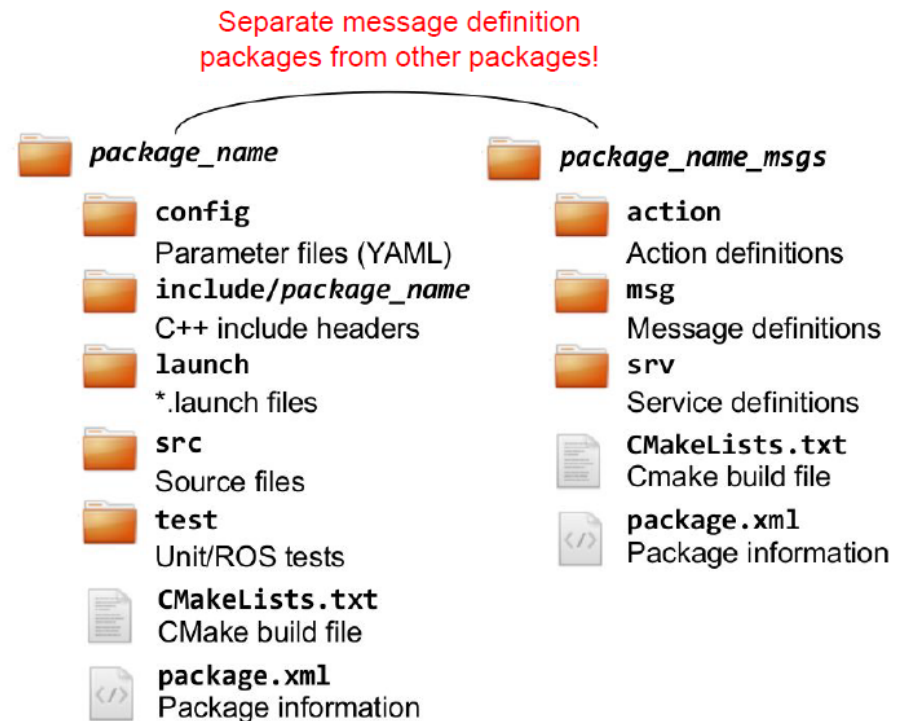
# ROS Package



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## ROS Packages

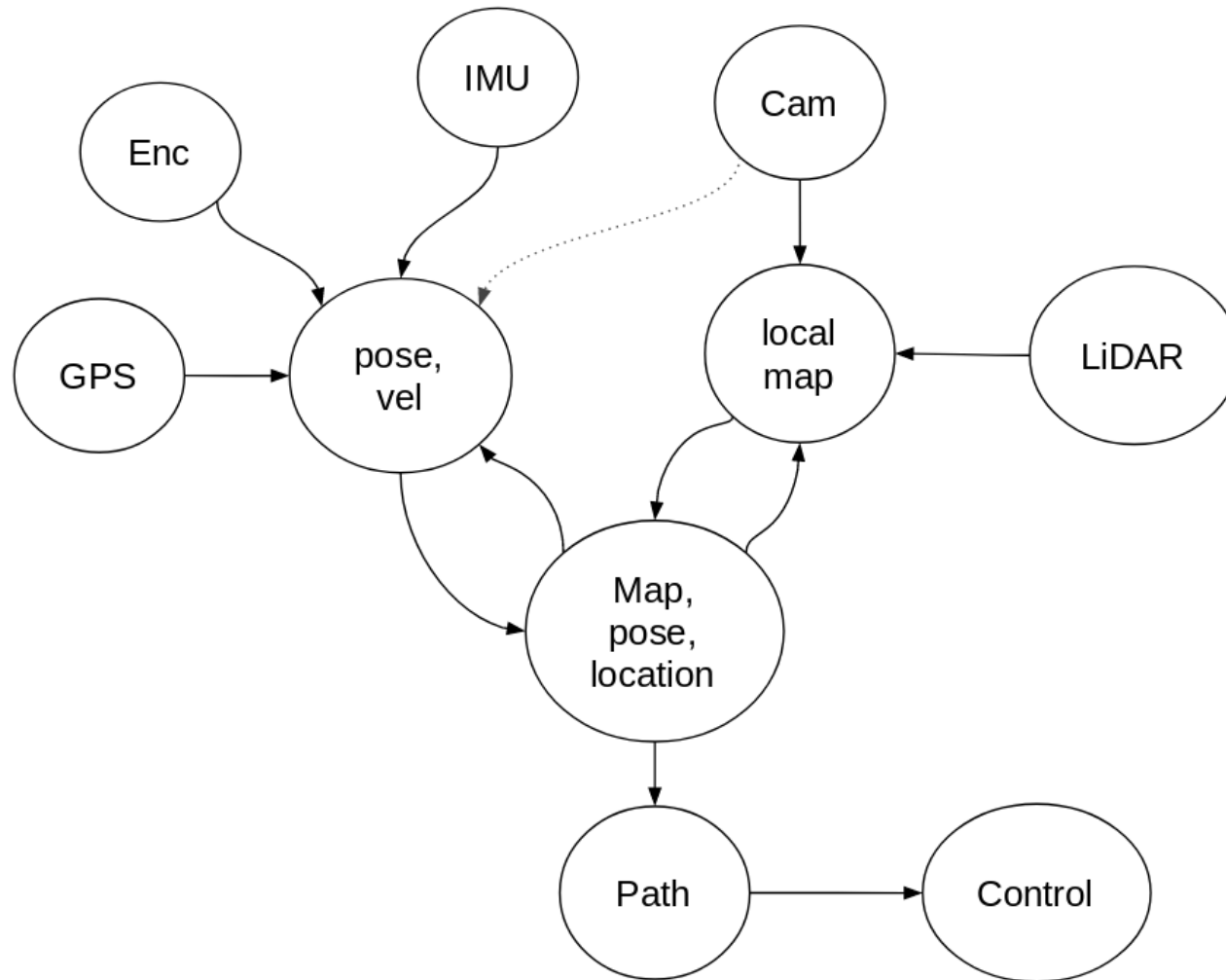
- ROS software is organized into packages, which can contain source code, launch files, configuration files, message definitions, data, and documentation
- A package that builds up on/requires other packages (e.g. message definitions), declares these as dependencies



# Software Architecture



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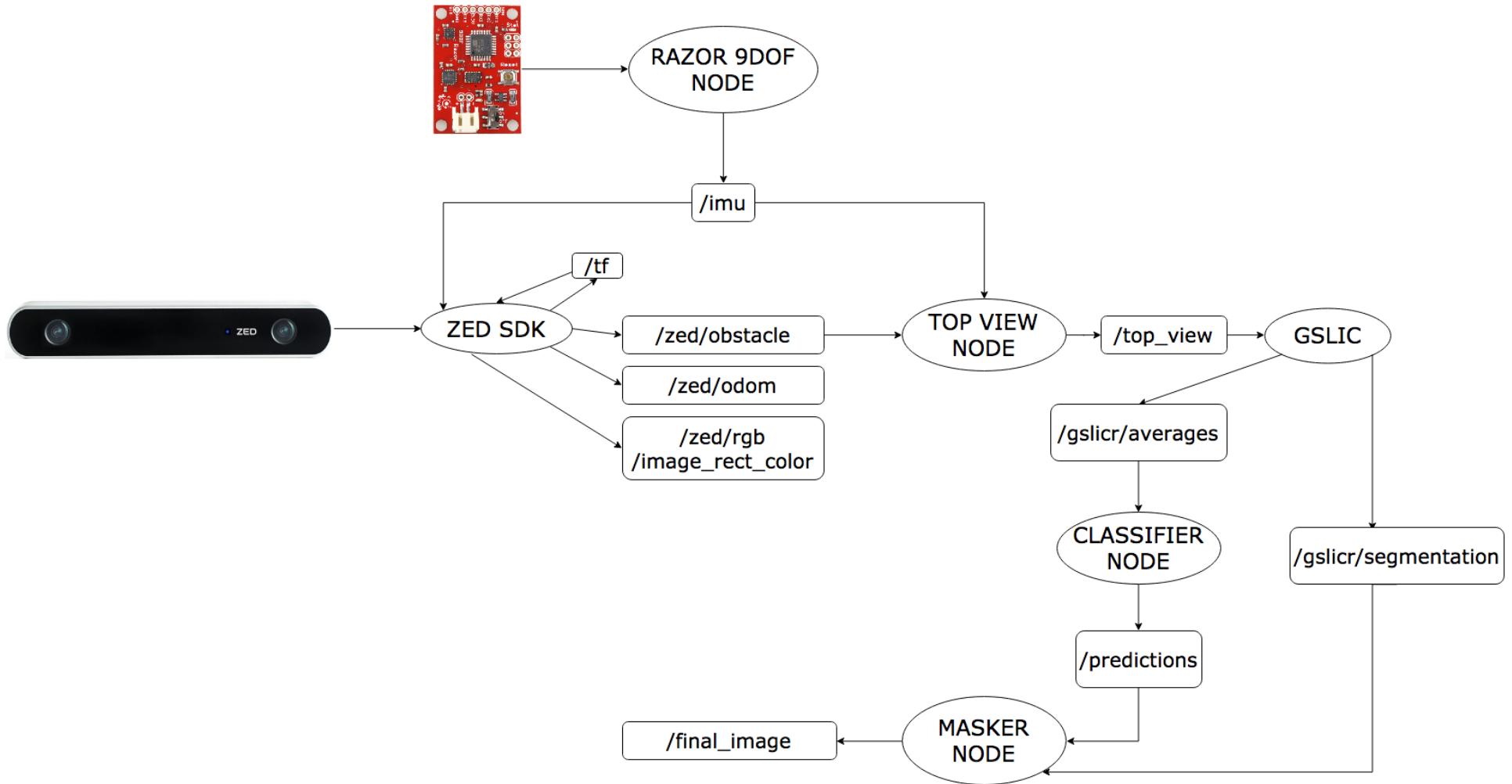




# Lane Detection: Computer Vision



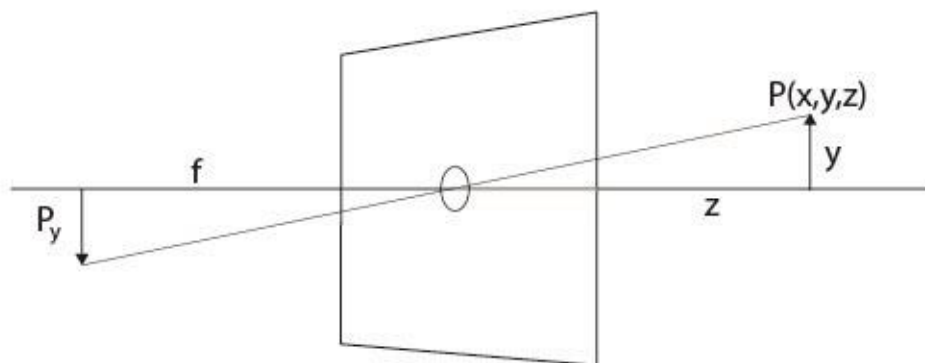
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# Pinhole Camera Model



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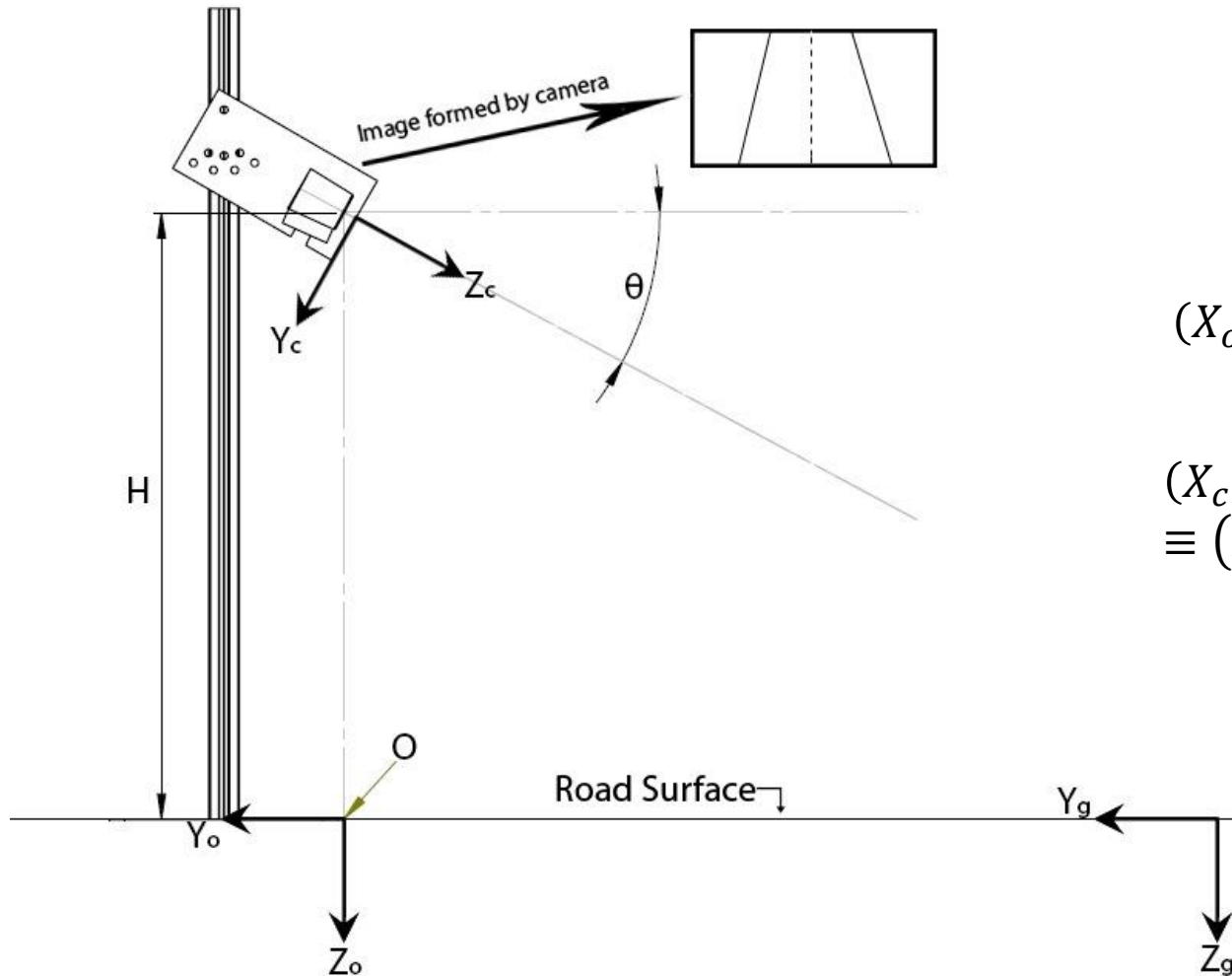
$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

$$x = \frac{x'}{w}, y = \frac{y'}{w}$$

# Inverse Perspective Transformation



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$$(X_f, Y_f, Z_f) \equiv \left( \frac{x_f}{s}, \frac{y_f}{s}, 0 \right)$$

$$(X_o, Y_o, Z_o) \equiv (X_f - O_x, Y_f - O_y, Z_f)$$

$$(X_c, Y_c, Z_c) \equiv (X_o, (H + Z_o) \cos(\theta) + Y_o \sin(\theta), H)$$

$$(x_c, y_c) \equiv \left( \frac{X_c}{Z_c} f_x + c_x, \frac{Y_c}{Z_c} f_y + c_y \right)$$

Lane following transformation

# Top View Transformation



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$$(x_c, y_c) \equiv \left( \frac{\left(\frac{x_f}{s} - O_X\right)}{H \sin(\theta) - \left(\frac{y_f}{s} - O_Y\right) \cos(\theta)} f_x + c_x, \frac{H \cos(\theta) + \left(\frac{y_f}{s} - O_Y\right) \sin(\theta)}{H \sin(\theta) - \left(\frac{y_f}{s} - O_Y\right) \cos(\theta)} f_y + c_y \right)$$

OpenCV implementation

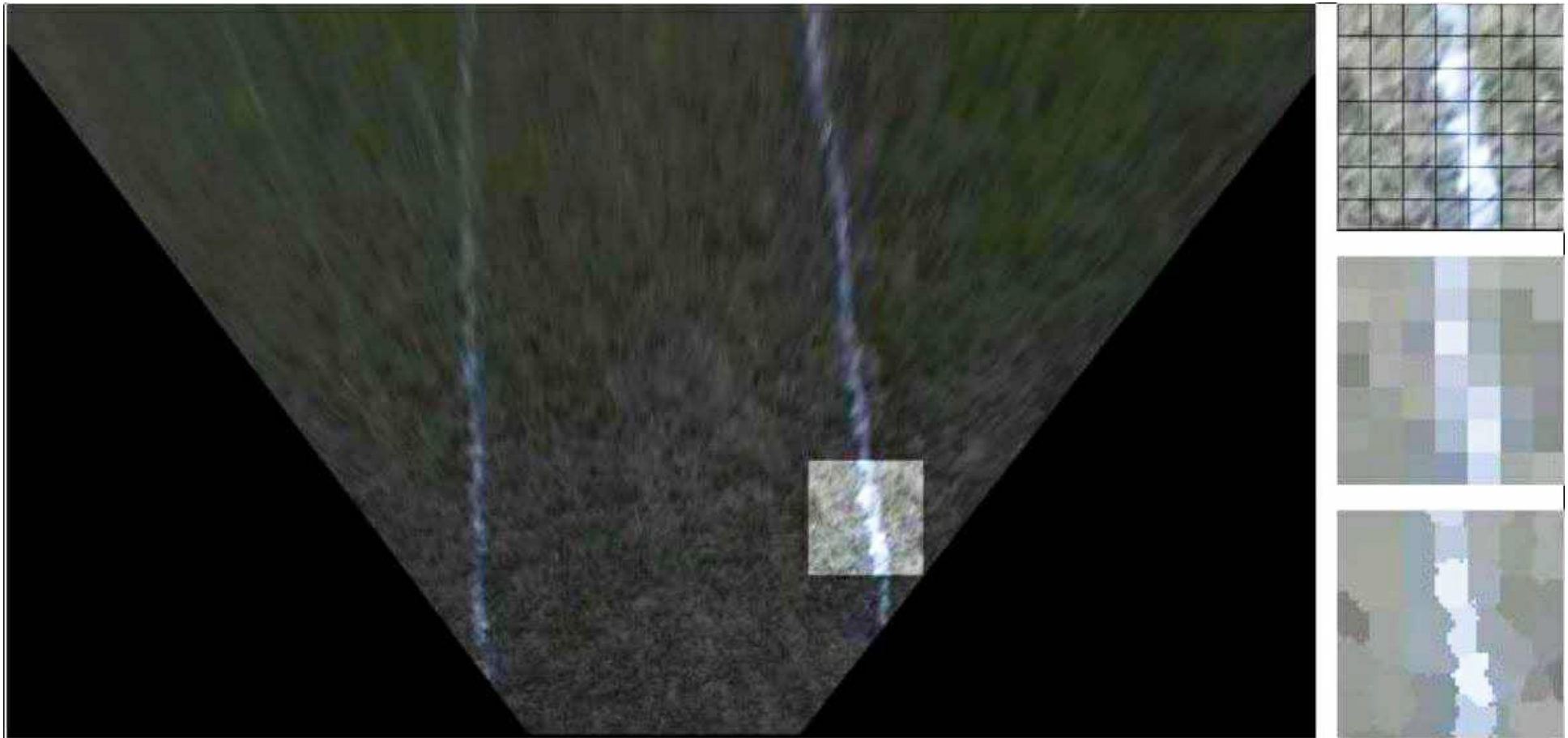
$$\text{dst}(x, y) = \text{src} \left( \frac{M_{11}x + M_{12}y + M_{13}}{M_{31}x + M_{32}y + M_{33}}, \frac{M_{21}x + M_{22}y + M_{23}}{M_{31}x + M_{32}y + M_{33}} \right)$$

Ref: [https://docs.opencv.org/2.4/modules/imgproc/doc/geometric\\_transformations.html#warperspective](https://docs.opencv.org/2.4/modules/imgproc/doc/geometric_transformations.html#warperspective)

# Super-Pixel Segmentation



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Reducing the dimensionality of data without loss of important information

# Super-Pixel Segmentation

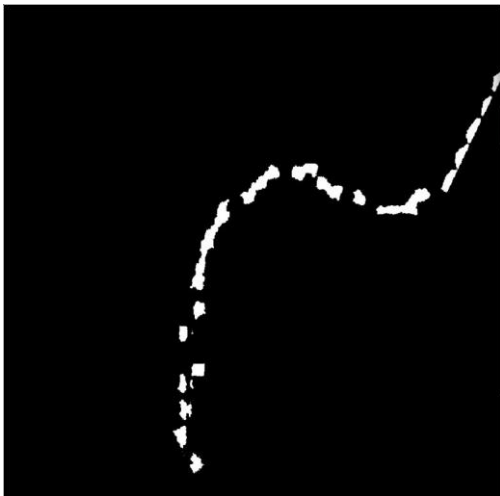
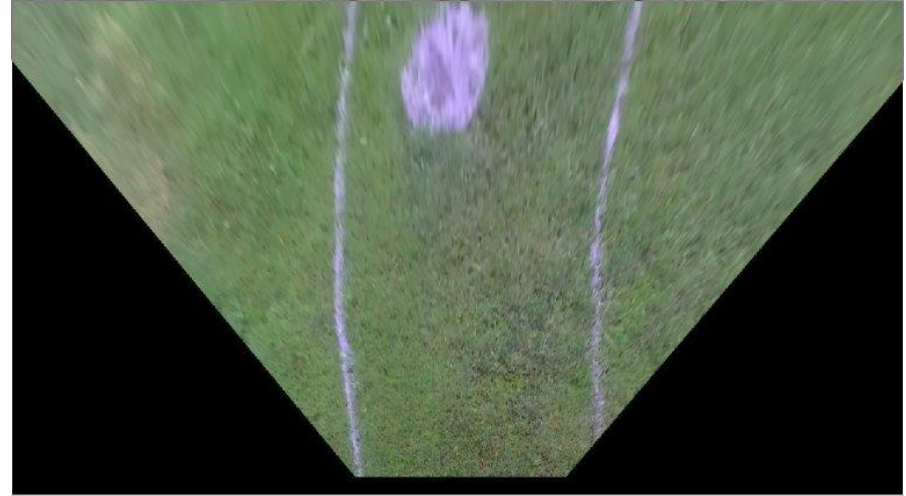
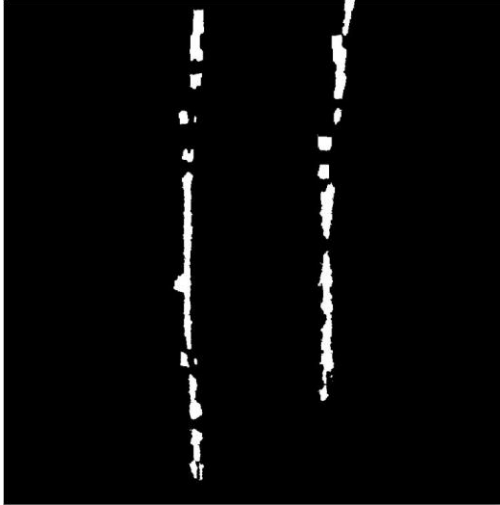


I I T K A N P U R

- Performing an unsupervised algorithm for image clustering
- Using an open Source and GPU accelerated implementation of SLIC (Simple Linear Iterative Clustering )
- SLIC divides the image into segments based on 5 dimensional distance
- Three dimensions are for RGB colors and 2 dimensions are for XY coordinates

# Lane Detection

I I T K A N P U R





# Obstacle Detection

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- Obstacle detection is done using the depth from stereo camera
- Alternatively, Lidar is used for avoidance

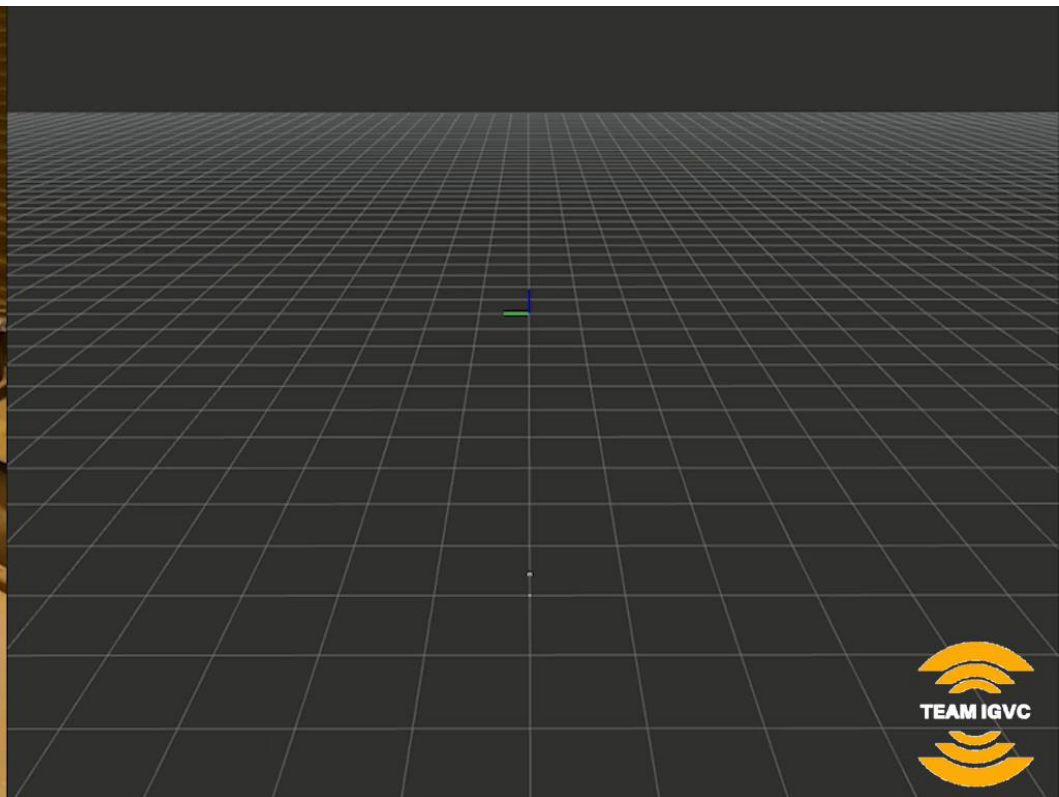




# Indoor Navigation

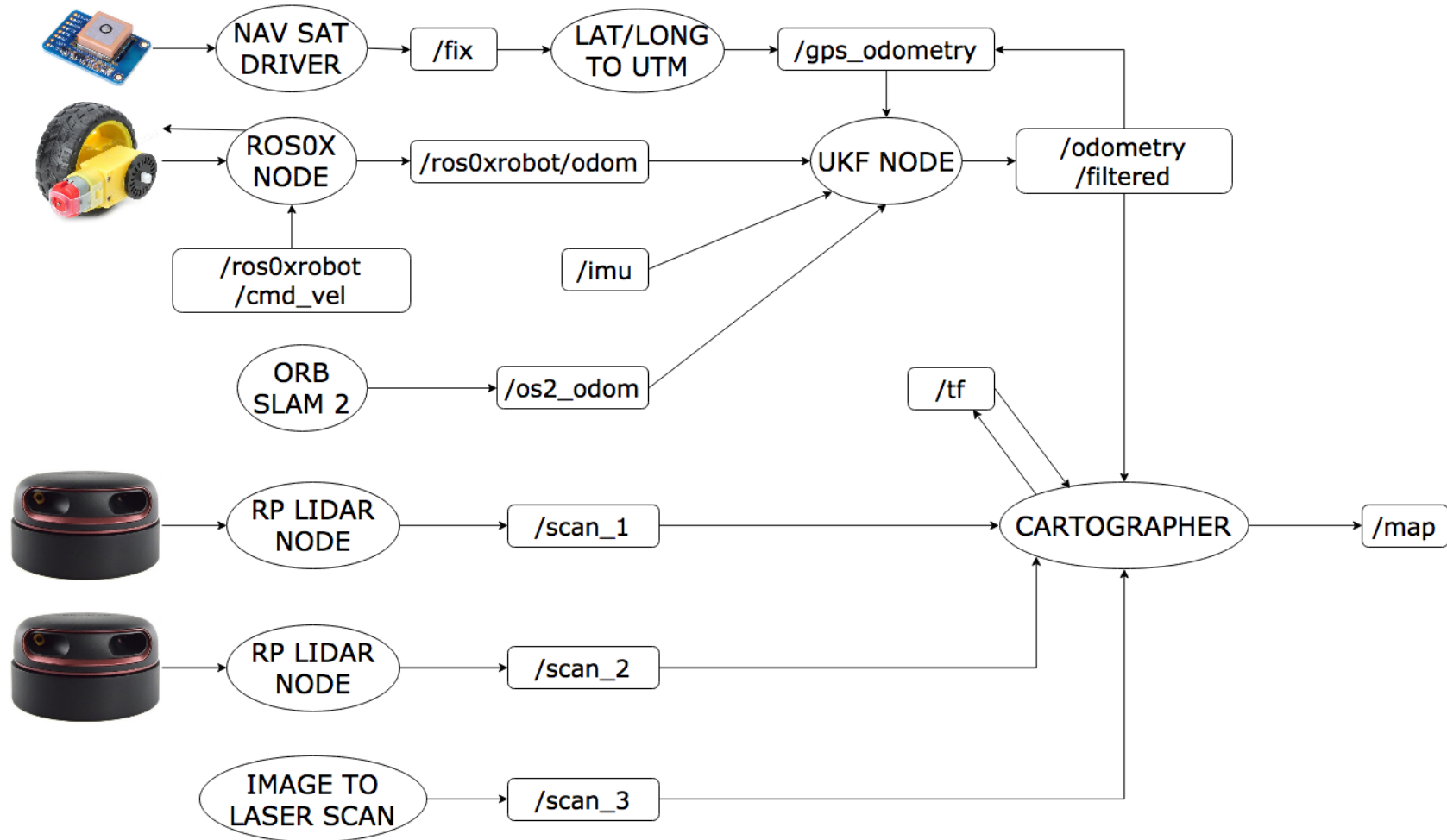


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# Simultaneous Localization and Mapping

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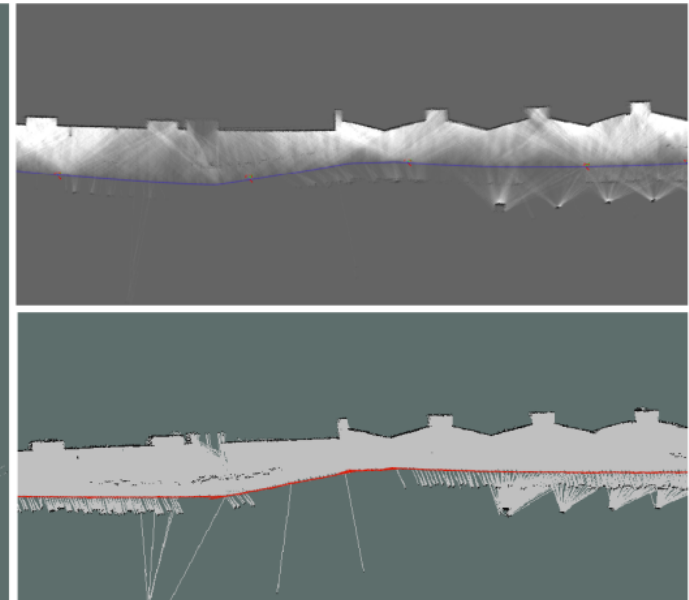
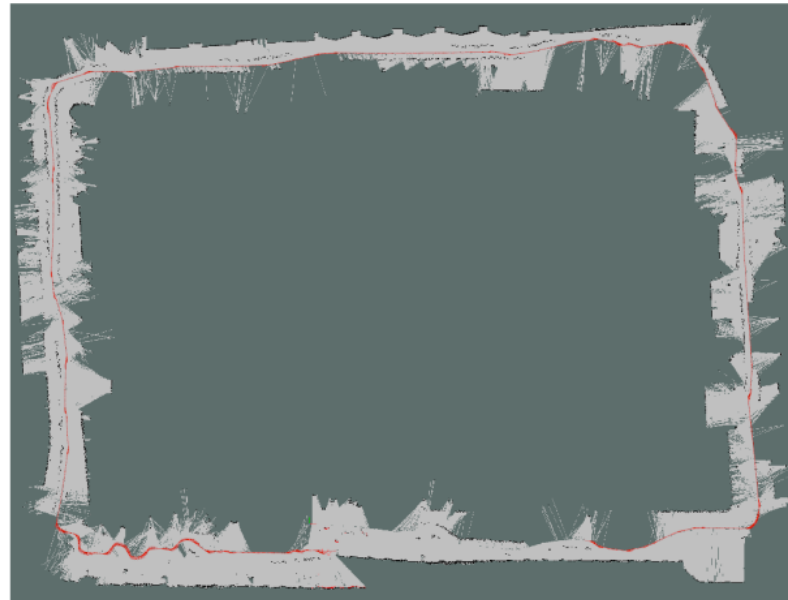


# Simultaneous Localization and Mapping



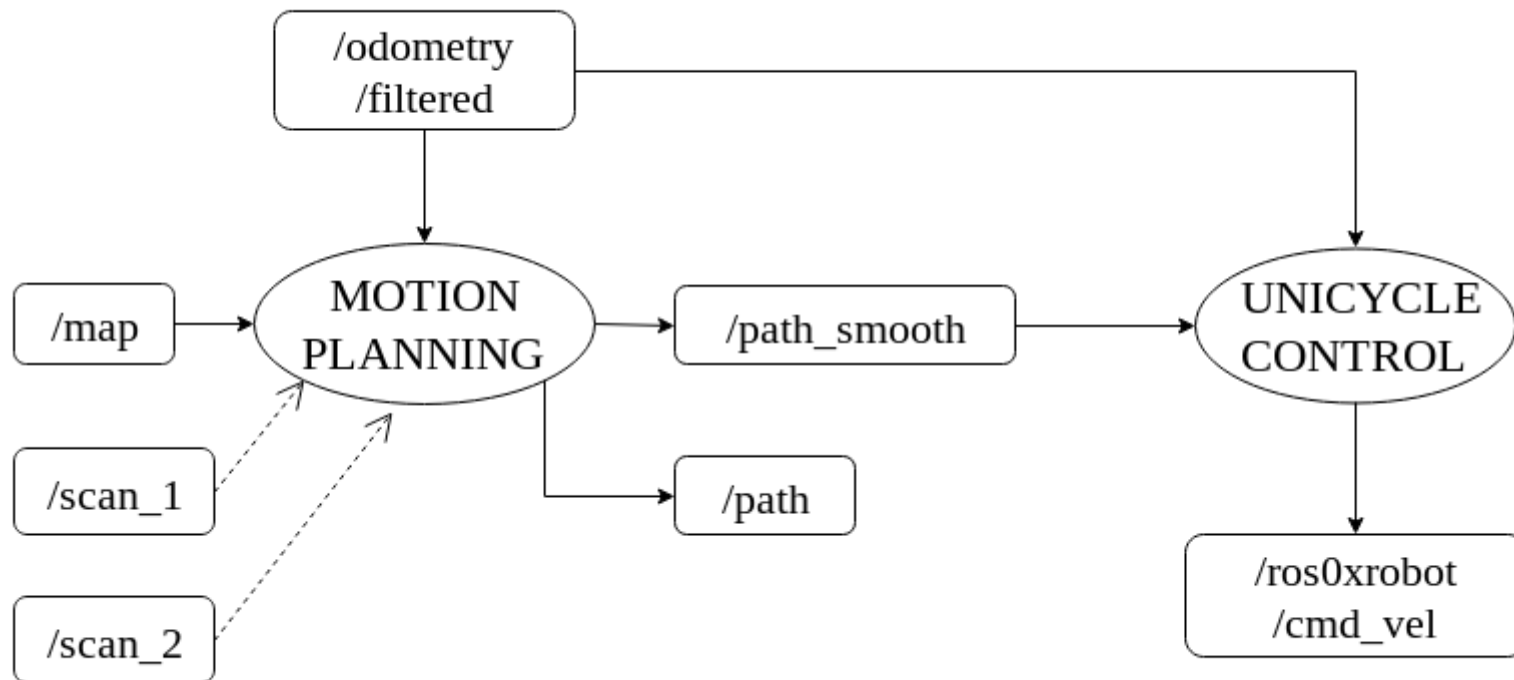
I I T K A N P U R

- UKF
- Cartographer
- Odometry



# Motion Planning and Control

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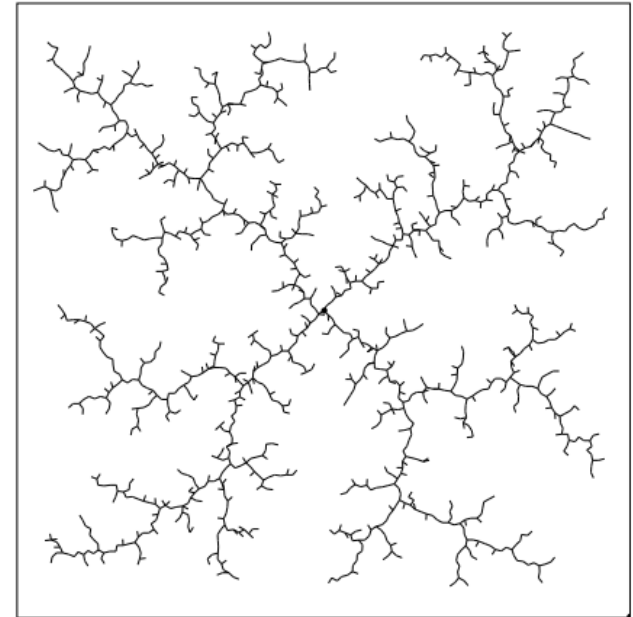
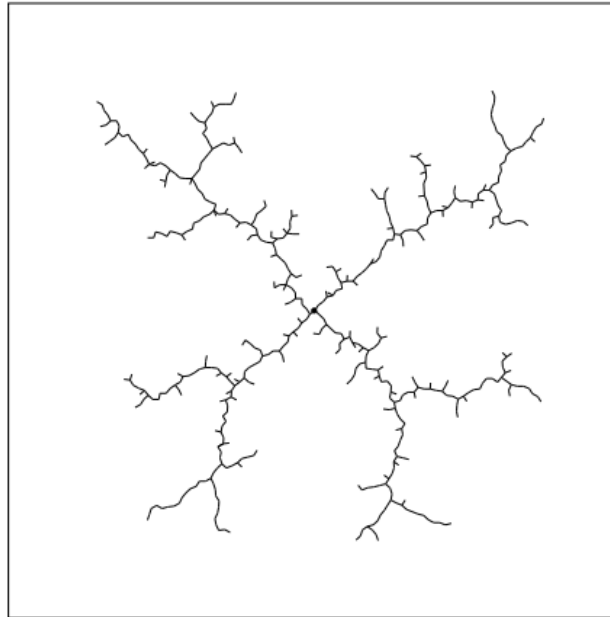
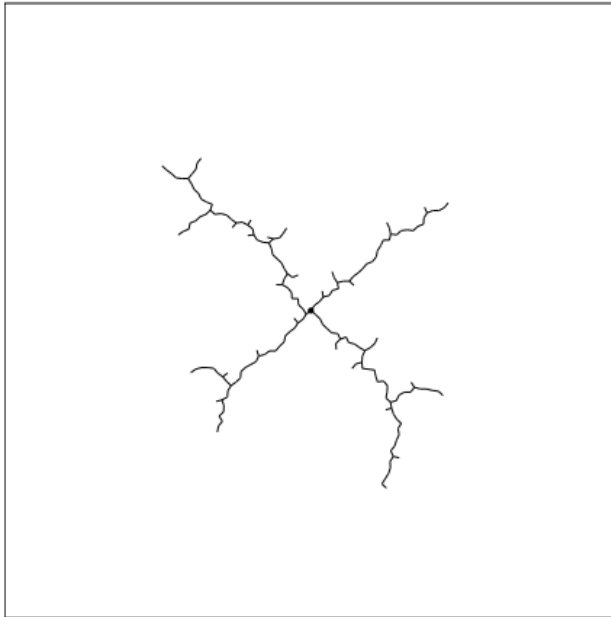


# Sampling-based Algorithm



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## Path planning using modified RRT

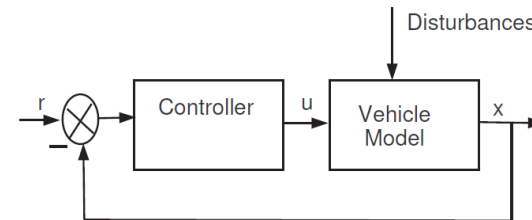
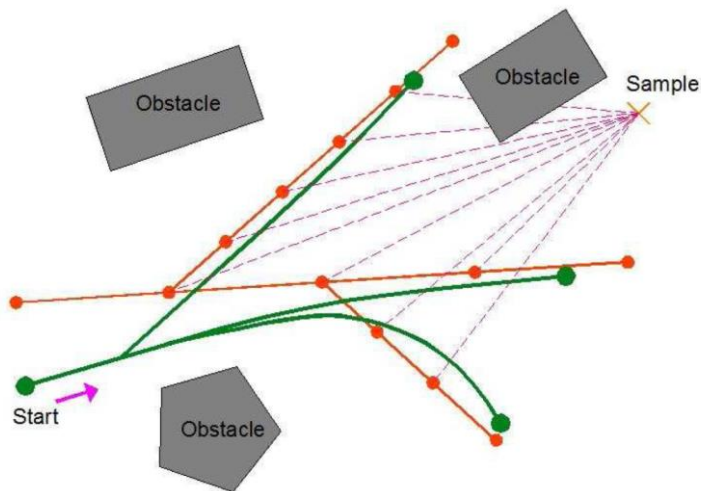


# Chance constrained RRT (CC-RRT) Algorithm



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- Grow a tree of state distributions for a given time
  - sample reference path (similar to waypoint selection)
  - generate trajectory for the sampled path (use a control/guidance law to generate trajectory)
  - evaluate the feasibility of the generated trajectory (using chance constraint)
  - include the path in the existing tree if it is feasible

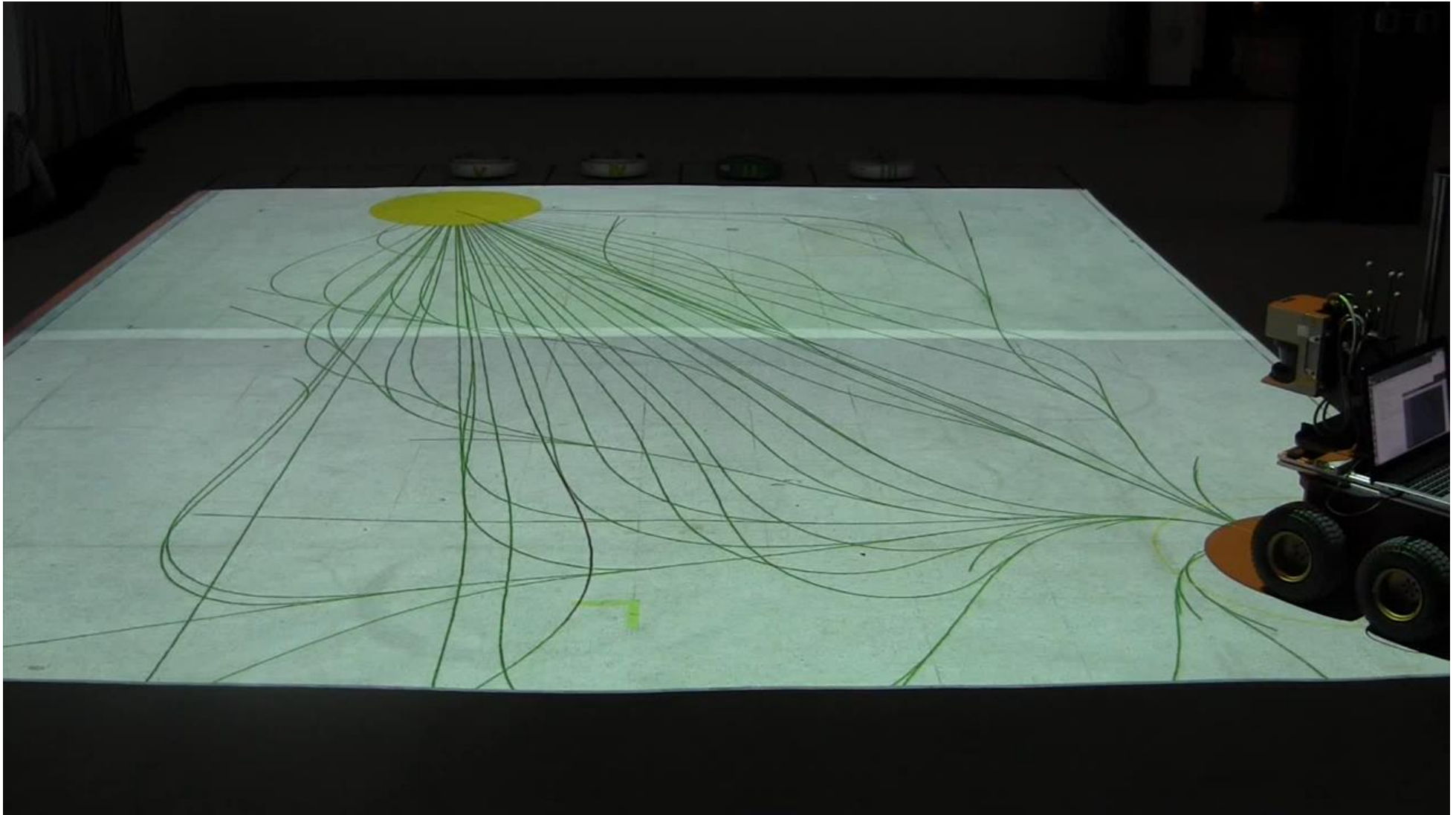




# Robust:ACL@MIT



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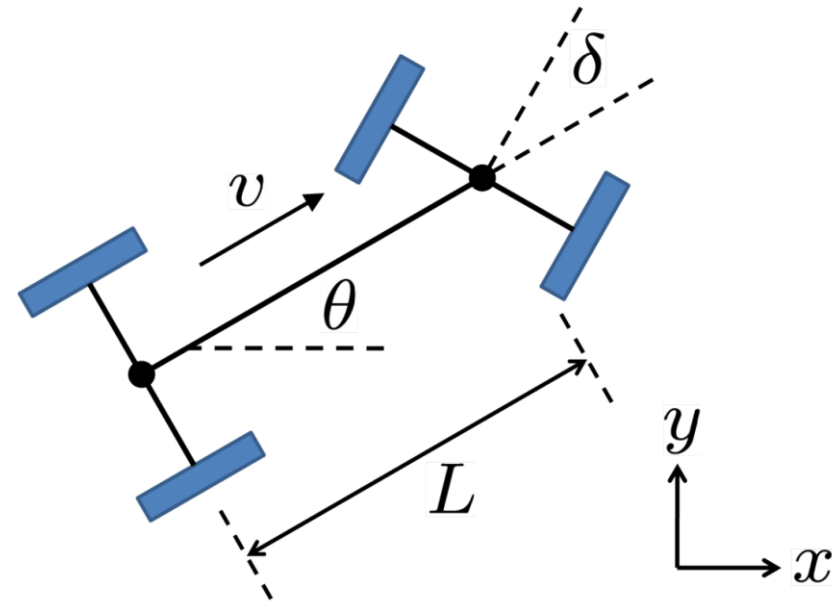


# Kinematic Model: Ackerman Steering



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$$\begin{aligned}\dot{x} &= v \cos \theta, \\ \dot{y} &= v \sin \theta, \\ \dot{\theta} &= \frac{v}{L} \tan \delta.\end{aligned}$$



Explicit steering vehicle model

$$\begin{aligned}\dot{\delta} &= \frac{1}{T_{\delta}} (\delta_R - \delta), \\ \dot{v} &= a, \\ \dot{a} &= \frac{1}{T_a} (a_R - a),\end{aligned}$$



# Skid Steering Model



I I T K A N P U R

$$\dot{x} = v \cos \theta,$$

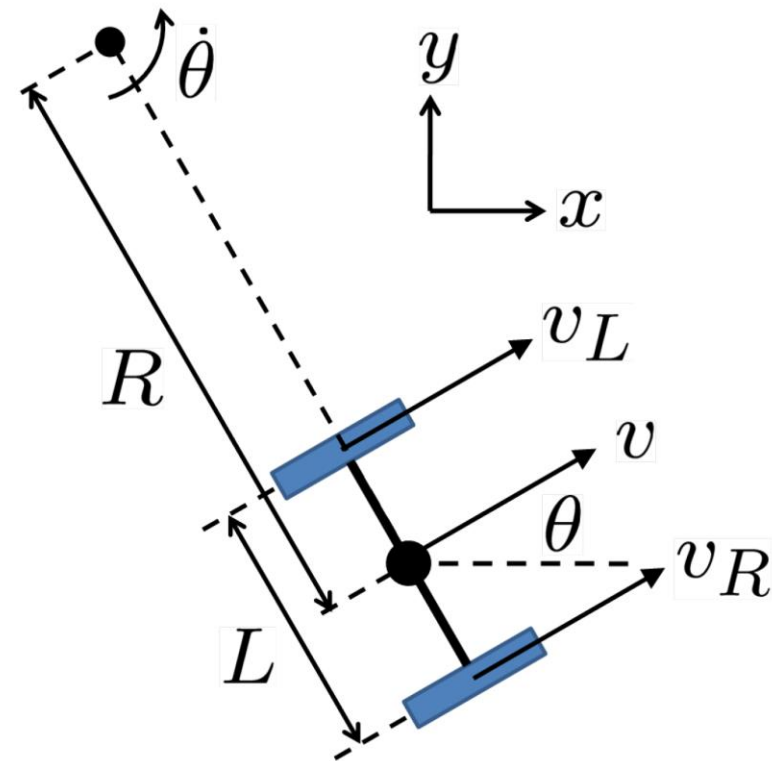
$$\dot{y} = v \sin \theta,$$

$$\dot{\theta} = \frac{\Delta v}{L}.$$

$$\dot{x} = \frac{1}{2} v_R \cos \theta + \frac{1}{2} v_L \cos \theta,$$

$$\dot{y} = \frac{1}{2} v_R \sin \theta + \frac{1}{2} v_L \sin \theta,$$

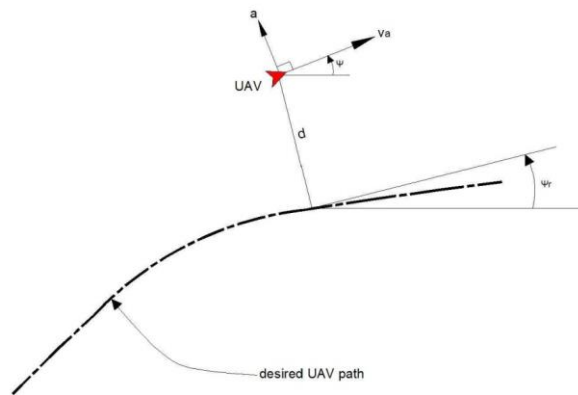
$$\dot{\theta} = \frac{1}{L} v_R - \frac{1}{L} v_L.$$



# Path Following Problem



I I T K A N P U R



- Calculate lateral acceleration

$$\begin{aligned} \text{(i)} \quad & \lim_{t \rightarrow \infty} d = 0, \\ \text{(ii)} \quad & \lim_{t \rightarrow \infty} \tilde{\psi} = 0, \\ \text{(iii)} \quad & |u| \leq u_{max}. \end{aligned}$$

# Mathematical Formulation



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kinematic model

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\psi} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} v_a \cos \psi \\ v_a \sin \psi \\ \frac{g}{v_a} \tan \phi \\ -k(\phi - \phi^d) \end{bmatrix}$$

Path following law: pursuit and LOS components

$$\phi^d = \tan^{-1} \left( \frac{k_1(\psi_r - \psi) + k_2 d}{g} \right)$$

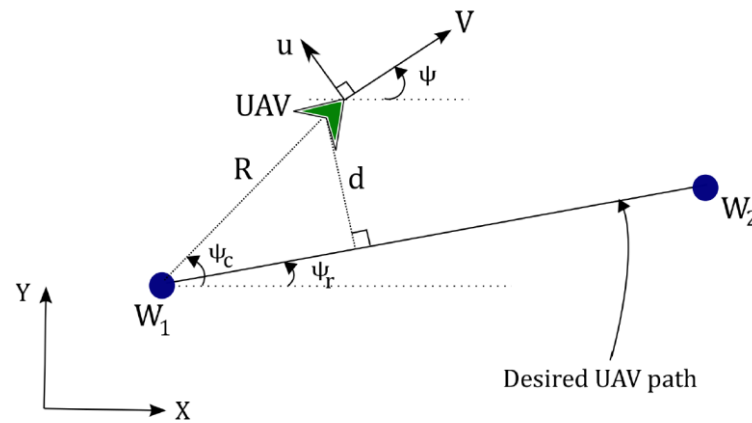
Error dynamics

$$\begin{aligned} \dot{d} &= v_a \sin(\psi_r - \psi) \\ \dot{\psi} &= -\frac{k_1}{v_a}(\psi_r - \psi) - \frac{k_2}{v_a} d \end{aligned}$$

# Straight Line following



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$$d = R \sin(\psi_c - \psi_r)$$

$$\tilde{\psi} = \psi - \psi_r$$

# Circle following

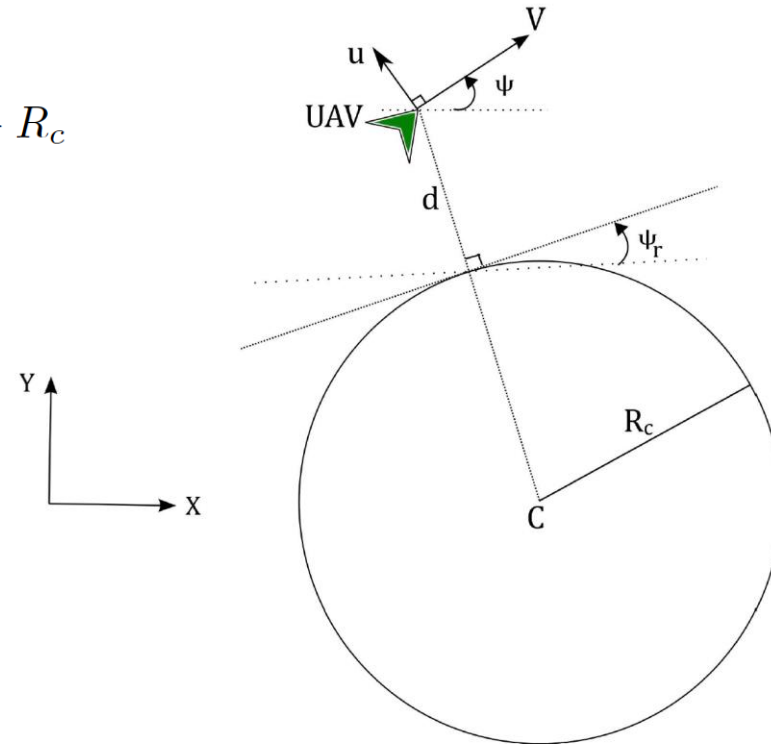


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$$d = \sqrt{(x - x_c)^2 + (y - y_c)^2} - R_c$$

$$\tilde{\psi} = \psi - \psi_r$$

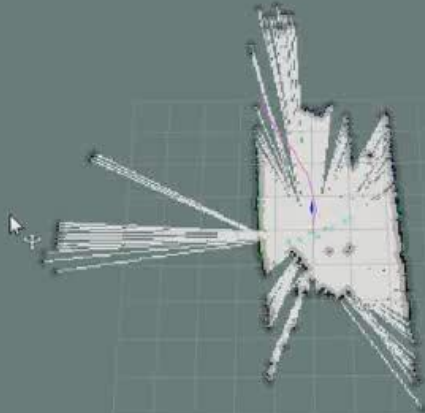
$$\psi_r = \tan^{-1} \frac{y_c - y}{x_c - x} \pm \frac{\pi}{2}$$



# SLAM and Motion Planning



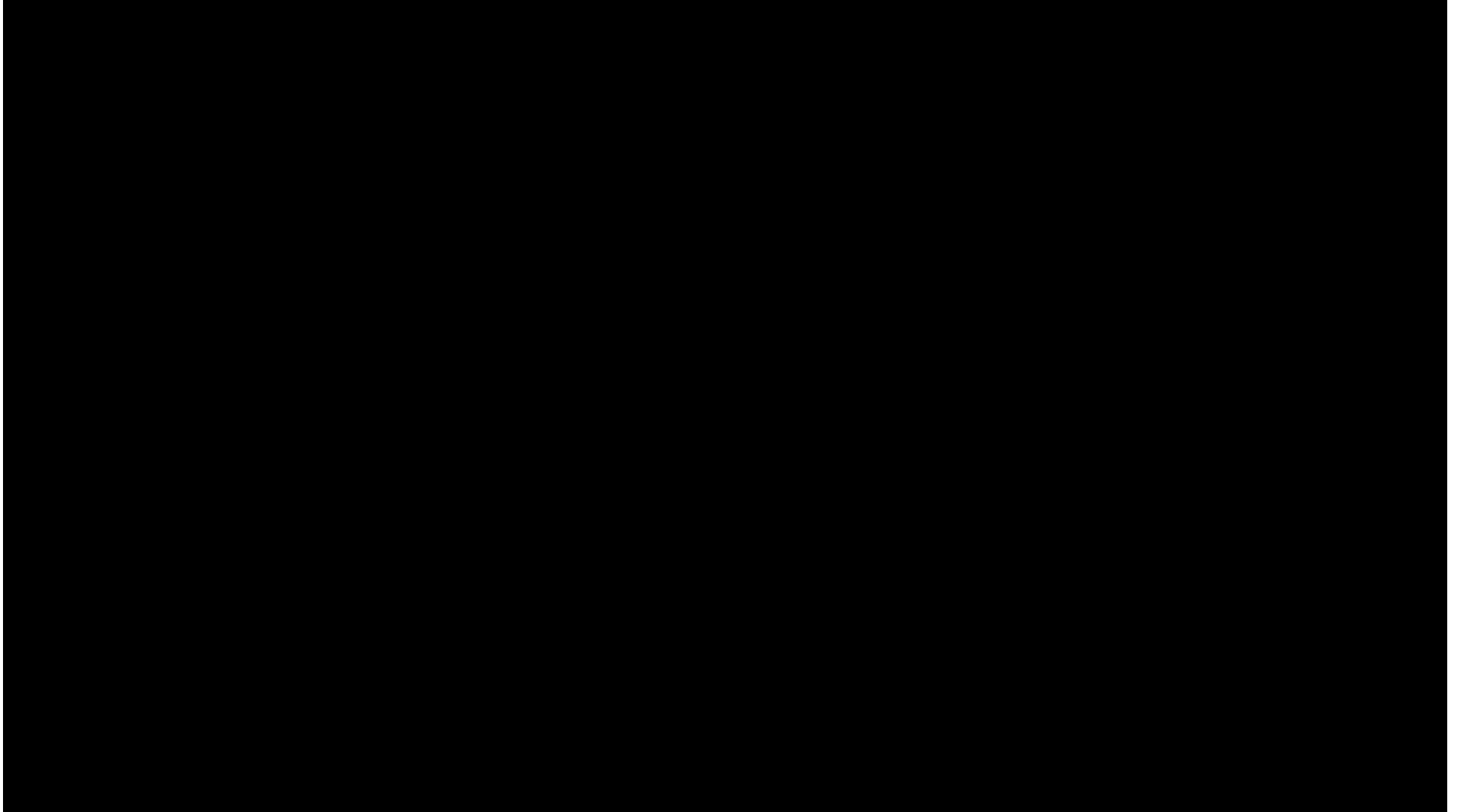
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# Vision based Autonomous Tracking and Landing



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# Acknowledgement



I I T K A N P U R

- **IGVC Team**
- **Harsh Sinha, Shubh Gupta, Swati Gupta, Deepak Gangwar**
- **Aalap Saha, Hemanth Bollamreddi, Abhishek Yadav, Vaibhav Agarwal, Vardhan Gupta**



# Thanks



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